

Problem 24: Number of Digits

Given two natural numbers x and k , compute the number of digits needed to represent x in base- k .

$$\begin{aligned} A &= \mathbb{N} \times \mathbb{N} \times \mathbb{N} \\ &\quad x \quad k \quad d \\ B &= \mathbb{N} \times \mathbb{N} \\ &\quad x' \quad k' \\ Q &= (x' = x) \wedge (k' = k) \\ R &= Q \wedge k^d < x \leq k^{d-1} \end{aligned}$$